

worksheet 3.3 page 1

$$l := 10 \text{ m}$$

$$X1 := 0 \text{ m}$$

$$Y1 := 0 \text{ m}$$

$$R1 := 1.5 \cdot 10^{-3} \text{ } \Omega$$

$$n_1 := 30$$

$$N := n_1 + n_2 + n_3$$

$$i := 1 .. n_1$$

$$\theta_i := \frac{2 \cdot \pi}{n_1} \cdot (i - 0.5) \text{ radian}$$

$$x_i := X1 + R1 \cdot \cos(\theta_i)$$

$$y_i := Y1 + R1 \cdot \sin(\theta_i)$$

$$r_i := \frac{R1}{n_1}$$

$$i := n_1 + 1 .. n_1 + n_2$$

$$\theta_i := \frac{2 \cdot \pi}{n_2} \cdot (i - n_1 - 0.5)$$

$$x_i := X2 + R2 \cdot \cos(\theta_i)$$

$$y_i := Y2 + R2 \cdot \sin(\theta_i)$$

$$r_i := \frac{R2}{n_2}$$

$$i := n_1 + n_2 + 1 .. N$$

$$\theta_i := \frac{2 \cdot \pi}{n_3} \cdot (i - n_1 - n_2 - 0.5)$$

$$x_i := X3 + R3 \cdot \cos(\theta_i)$$

$$y_i := Y3 + R3 \cdot \sin(\theta_i)$$

$$r_i := \frac{R2}{n_3}$$

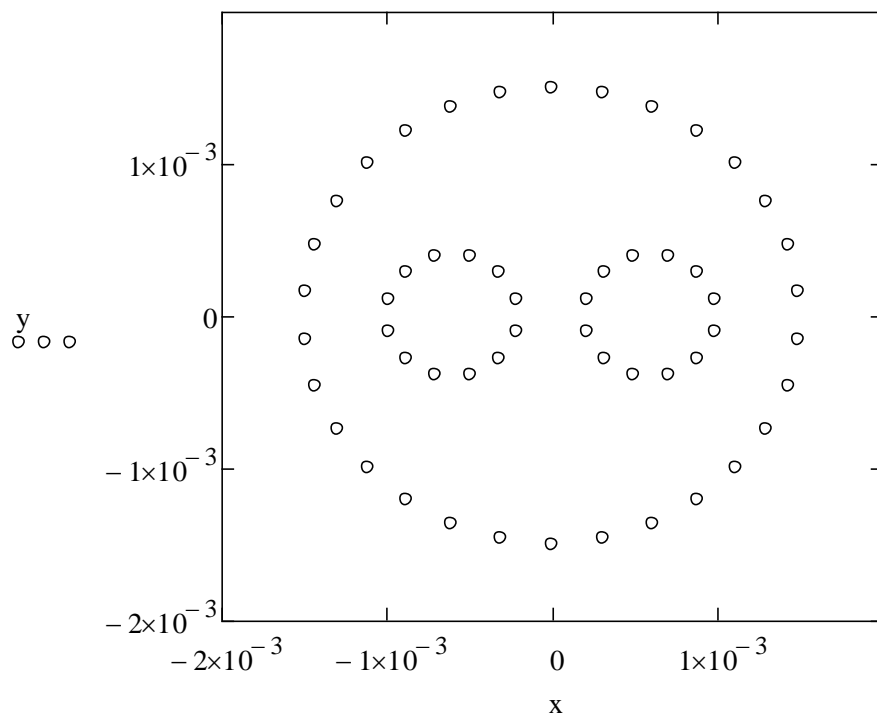


Fig 3.3.1 Definition of elemental conductors

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$$\mu_o := 4 \cdot \pi \cdot 10^{-7} \text{ H/m}$$

$$\mu_r := 1$$

$$\underline{K} := \frac{\mu_o \cdot \mu_r \cdot l}{2 \cdot \pi} = 2 \times 10^{-6} \text{ H}$$

$$\text{Zp} := \left| \begin{array}{l} \text{for } i \in 1 \dots N \\ \quad \text{for } j \in 1 \dots N \\ \quad \quad h \leftarrow x_j - x_i \\ \quad \quad v \leftarrow y_j - y_i \\ \quad \quad \text{rad} \leftarrow \sqrt{h^2 + v^2} \\ \quad \quad \text{rad} \leftarrow r_i \text{ if } \text{rad} = 0 \\ \quad \quad L_{p_i,j} \leftarrow K \cdot \ln\left(\frac{l}{\text{rad}}\right) \end{array} \right| L_p$$

$$\text{Zloop} := \left| \begin{array}{l} \text{for } i \in 1 \dots N - 1 \\ \quad \text{for } j \in 1 \dots N - 1 \\ \quad \quad L_{loop_i,j} \leftarrow Z_{p_i,j} - Z_{p_i,j+1} - Z_{p_{i+1},j} + Z_{p_{i+1},j+1} \end{array} \right| L_{loop}$$

$$\text{Vloop} := \left| \begin{array}{l} \text{for } i \in 1 \dots N - 1 \\ \quad \left| \begin{array}{l} V_i \leftarrow 0 \\ V_i \leftarrow 1 \text{ if } i = n_1 \end{array} \right. \end{array} \right| V$$

$$I_{loop} := \text{lsolve}(\text{Zloop}, \text{Vloop})$$

$$I_p := \left| \begin{array}{l} I_1 \leftarrow I_{loop_1} \\ \text{for } i \in 2 \dots N - 1 \\ \quad I_i \leftarrow I_{loop_i} - I_{loop_{i-1}} \\ I_N \leftarrow -I_{loop_{N-1}} \end{array} \right| I$$

worksheet page 2: Calculating currents in elemental conductors

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(worksheet 3.3 page 2 is identical to figure 3.2.6)

$$n = \begin{pmatrix} 30 \\ 12 \\ 12 \end{pmatrix}$$

number of elemental conductors
in each composite.

$$\text{Start} := \begin{pmatrix} 1 \\ n_1 + 1 \\ n_1 + n_2 + 1 \end{pmatrix} \quad \text{End} := \begin{pmatrix} n_1 \\ n_1 + n_2 \\ N \end{pmatrix}$$

Pointers to nine sub-matrices.

$$h := 1 \dots 3 \quad k := 1 \dots 3$$

control variables

$$vq_{h,k} := \left| \begin{array}{l} v \leftarrow 0 \\ \text{for } i \in \text{Start}_h \dots \text{End}_h \\ \quad \text{for } j \in \text{Start}_k \dots \text{End}_k \\ \quad \quad v \leftarrow v + Z_{p_i,j} \cdot I_{p_j} \\ \frac{v}{n_h} \end{array} \right|$$

voltage components of sub-matrices

$$vq = \begin{pmatrix} 12.667 & -6.334 & -6.334 \\ 12.694 & -7.284 & -6.41 \\ 12.694 & -6.41 & -7.284 \end{pmatrix}$$

$$Vq_h := \left| \begin{array}{l} v \leftarrow 0 \\ \text{for } k \in 1 \dots 3 \\ \quad v \leftarrow v + vq_{h,k} \\ v \end{array} \right|$$

Voltage along composite conductors:-

$$Vq = \begin{pmatrix} -5.874 \times 10^{-8} \\ -1 \\ -1 \end{pmatrix}$$

$$Iq_h := \left| \begin{array}{l} I \leftarrow 0 \\ \text{for } i \in \text{Start}_h \dots \text{End}_h \\ \quad I \leftarrow I + I_{p_i} \\ I \end{array} \right|$$

Current in composite conductors:-

$$Iq = \begin{pmatrix} 7.193 \times 10^5 \\ -3.597 \times 10^5 \\ -3.597 \times 10^5 \end{pmatrix}$$

$$I_{\text{total}} := Iq_1 + Iq_2 + Iq_3 = 0$$

Sum of currents in conductors

Figure 3.3.2 Computing values for voltages and currents in composite conductors.

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$$L_{qh,k} := \frac{v_{qh,k}}{I_{qk}}$$

Deriving primitive inductance values from current and voltage data. See equation (3.2.15)

$$L_q = \begin{pmatrix} 1.761 \times 10^{-5} & 1.761 \times 10^{-5} & 1.761 \times 10^{-5} \\ 1.765 \times 10^{-5} & 2.025 \times 10^{-5} & 1.782 \times 10^{-5} \\ 1.765 \times 10^{-5} & 1.782 \times 10^{-5} & 2.025 \times 10^{-5} \end{pmatrix}$$

Deriving loop inductance values for three-conductor assembly. See equation (3.2.3)

$$L_{\text{loop}} := \begin{array}{|l} \text{for } h \in 1..2 \\ \quad \text{for } k \in 1..2 \\ \quad \quad L_{h,k} \leftarrow L_{qh,k} - L_{qh,k+1} - L_{qh+1,k} + L_{qh+1,k+1} \\ \mathbf{L} \end{array}$$

$$L_{\text{loop}} = \begin{pmatrix} 2.606 \times 10^{-6} & -2.432 \times 10^{-6} \\ -2.432 \times 10^{-6} & 4.864 \times 10^{-6} \end{pmatrix}$$

$$L_{c1} := L_{\text{loop}1,1} + L_{\text{loop}1,2}$$

$$L_{c2} := -L_{\text{loop}1,2}$$

$$L_{c3} := L_{\text{loop}2,2} + L_{\text{loop}2,1}$$

Deriving circuit inductors for three-conductor assembly. See equation (2.7.10).

$$\frac{L_c}{2} = \begin{pmatrix} 8.711 \times 10^{-8} \\ 1.216 \times 10^{-6} \\ 1.216 \times 10^{-6} \end{pmatrix} \quad \text{H}$$

$$\epsilon_o := 8.854 \cdot 10^{-12} \quad \text{F/m}$$

$$\epsilon_r := 1$$

$$C_c := \frac{\mu_o \cdot \mu_r \cdot \epsilon_o \cdot \epsilon_r \cdot l^2}{L_c}$$

Deriving capacitor values. See equation (2.3.3)

$$C_c = \begin{pmatrix} 6.386 \times 10^{-9} \\ 4.575 \times 10^{-10} \\ 4.575 \times 10^{-10} \end{pmatrix} \quad \text{F}$$

Figure 3.3.3 Calculating values of circuit components

$$i := 1..N \qquad A_{i,1} := \mathbf{x}_i \cdot 10^3 \qquad A_{i,2} := \mathbf{y}_i \cdot 10^3 \qquad A_{i,3} := |\mathbf{I}\mathbf{p}_i| \cdot 10^{-3}$$

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